

Table 5.1. Spherical harmonics $Y_{lm}(\theta, \varphi)$ for $l = 0, 1, 2, 3$

$Y_{00} = \left(\frac{1}{4\pi}\right)^{1/2}$	$Y_{30} = \left(\frac{7}{16\pi}\right)^{1/2} (5 \cos^3 \theta - 3 \cos \theta)$
$Y_{10} = \left(\frac{3}{4\pi}\right)^{1/2} \cos \theta$	$Y_{3,\pm 1} = \mp \left(\frac{21}{64\pi}\right)^{1/2} \sin \theta (5 \cos^2 \theta - 1) e^{\pm i\varphi}$
$Y_{1,\pm 1} = \mp \left(\frac{3}{8\pi}\right)^{1/2} \sin \theta e^{\pm i\varphi}$	$Y_{3,\pm 2} = \left(\frac{105}{32\pi}\right)^{1/2} \sin^2 \theta \cos \theta e^{\pm 2i\varphi}$
$Y_{20} = \left(\frac{5}{16\pi}\right)^{1/2} (3 \cos^2 \theta - 1)$	$Y_{3,\pm 3} = \mp \left(\frac{35}{64\pi}\right)^{1/2} \sin^3 \theta e^{\pm 3i\varphi}$
$Y_{2,\pm 1} = \mp \left(\frac{15}{8\pi}\right)^{1/2} \sin \theta \cos \theta e^{\pm i\varphi}$	
$Y_{2,\pm 2} = \left(\frac{15}{32\pi}\right)^{1/2} \sin^2 \theta e^{\pm 2i\varphi}$	

Table 6.1. Radial functions R_{nl} for the hydrogen-like atom for $n = 1$ to 6. The variable ρ is given by $\rho = 2Zr/na_\mu$

$$R_{10} = 2(Z/a_\mu)^{3/2} e^{-\rho/2}$$

$$R_{20} = \frac{(Z/a_\mu)^{3/2}}{2\sqrt{2}} (2 - \rho) e^{-\rho/2}$$

$$R_{21} = \frac{(Z/a_\mu)^{3/2}}{2\sqrt{6}} \rho e^{-\rho/2}$$

$$R_{30} = \frac{(Z/a_\mu)^{3/2}}{9\sqrt{3}} (6 - 6\rho + \rho^2) e^{-\rho/2}$$

$$R_{31} = \frac{(Z/a_\mu)^{3/2}}{9\sqrt{6}} (4 - \rho) \rho e^{-\rho/2}$$

$$R_{32} = \frac{(Z/a_\mu)^{3/2}}{9\sqrt{30}} \rho^2 e^{-\rho/2}$$

$$R_{40} = \frac{(Z/a_\mu)^{3/2}}{96} (24 - 36\rho + 12\rho^2 - \rho^3) e^{-\rho/2}$$

$$R_{41} = \frac{(Z/a_\mu)^{3/2}}{32\sqrt{15}} (20 - 10\rho + \rho^2) \rho e^{-\rho/2}$$

$$R_{42} = \frac{(Z/a_\mu)^{3/2}}{96\sqrt{5}} (6 - \rho) \rho^2 e^{-\rho/2}$$

$$R_{43} = \frac{(Z/a_\mu)^{3/2}}{96\sqrt{35}} \rho^3 e^{-\rho/2}$$