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Characterizing spatial-temporal forest fire patterns

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ABSTRACT

The spatial-temporal patterns of wildfire incidence and their relationship to various meteorological, geographical and geological variables is analyzed. Such relationships may be treated as components in separable point process models for wildfire activity. We show some of the techniques for the analysis of spatial point patterns that have become available due to recent developments in point process modelling software. These developments permit convenient exploratory data analysis, model fitting, and model assessment. The discussion of these techniques is conducted jointly with and in the context of some preliminary analyses of a collection of data sets which are of considerable interest in their own right. These data sets consist of the complete records of wildfires which occurred in

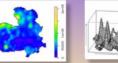
the third largest of Spain's autonomous regions, with a surface area of 79463 square kilometres (30681 sq mi), representing \$15.77% of the Spanis national territory. The total number of fires recorded in the study area during the period 1998-2007 is 8488. In addition to the locations of the fir centroids, we consider the following covariates and marks: (a) forest and vegetation ty humidity,...), (c) altitude, slope and orientation, (d) type of wildfire, and (e) time of occurrence



in the period 1998-2007







for the whole period 1998-2007





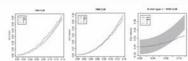


Results and Modeling forest fires

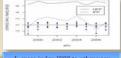
Forest fires can be regarded as spatio-temporal point patterns and thus space-time statistical tools can be of help in analyzing the behavior of fires ([6,8]). Additionally, forest fires represent a problem of considerable social importance worldwide. Investigation Forest ires can be regarded as spatio-temporal point patterns and thus space-time statistical tools can be of neigh an analyzing the behavior of lifes $\{(0,8)\}$. Additionally, forest tires represent a problem or considerates social importance worldwide. Investigation of the intensity is one of the first steps in analysing a point pattern. We are in particular interested in testing whether the point pattern the point pattern thus we fit an inhomogeneous Poisson process model with an intensity function which is log-linear on an observed covariate. In order to model the dependence of a point pattern on a spatial covariat, there are several requirements. First, the covariate must be a quantity Z(u) observable (in principle) at each location u in the window (e.g. altitude, slope, orientation). Such covariates may be continuous valued or factors (e.g. vegetation type). Second, the values $Z(x_i)$ of Z at each point of the data point pattern must be available. Thirdly, the values Z(u) as available. In addition to covariates there are other variables measured only at fire locations which are considered as marks. For example, fires are classified into two or more different types depending on the field size burned or on the cause starting the fire. In such cases, we may consider multitype point pattern. We have the continuous valued on the form of the K-function. Thus treatment of the homogeneous K-function where K-function is the homogeneous first the point K-function in the form of the K-function.



the four different types in Castilla La Mancha



Homogeneous K-function and envelopes under CSR for 1998; Middle: Inhomoge K-function for 1998; Right: Inhomogeneous K-function for 1998 and fire type 1



follows that, conditional on the number of events in any region A, the locations of the events form an adependent random sample from the uniform distribution on A. With this, a regular pattern is one in which events are more evenly spaced throughout A than would be expected under CSR, and typically arises through ome form of inhibitory dependence between events.

some form of infinition queenicance between events. Conversely, an aggregated pattern is one in which events tend to occur in closely spaced groups. Informally, the first-order and second-order properties of a point process ([9]) can be described by the (first-order) intensity function $\lambda(x)$, which is the point process analogue of the mean function for a real-valued stochastic process, and the second-order intensity function $\lambda(x)$, which is analogous to the covariance function of a real-valued process. The pair correlation function is defined as $g(x, y) = \lambda_2(x, y) / \lambda(x) \lambda(y)$.

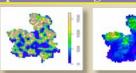
The process is stationary and isotropic if its statistical properties do not change under translation and rotation, respectively. If we now assume that the process is stationary and isotropic, the intensity function reduces to a constant, λ , equal to the expected number of events per unit area. In the nonstationary case, they are functions of the distance between points, or in the general case of the individual locations.

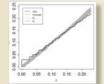
If the temporal argument is of interest, we may consider data in the form of a realization of a spatio-temporal point process within a finite spatio-temporal region. For many areas of application, a suitable point process

model must be able to accommodate spatial and/or temporal inhomogeneity. In this setting, a natural starting point for analysis of spatio-temporal point process data is to investigate the nature of any stochastic interactions among the points of the process after adjusting for spatial and/or temporal inhomogeneity. [9] introduced the *K-function* as a tool for data-analysis. One of its advantages over the pair correlation function is that it can be interpreted as a scaled expectation of an observable quantity. Specifically, let E(s) denote the expected number of further events within distance s of an arbitrary event. Then, $K(s) = \lambda^{-1}E(s)$. [3] extended definition of a reduced second moment measure, or K-function, to include a class of nonstationary processes.

HPP: homogeneous Poisson Process IPP: Inhomogeneous Poisson Process

Having all the previous descriptive information at hand, we propose several spatial point process models, univariate and multivariate taking into account the corresponding covariates and marks





L-index 2002 (polynom trend): Right: Inhomogeneous Matern claster L-index 2007 (trend: x, y and 4 covariates

Space-time modeling

Previous to finally consider the space-time structure, we first test for separability and then we propose a model for the space-time first-order intensity function. Cox processes are very useful for modelling aggregated point patterns, in particular in the spatial case where the two main classes of models are log-Gaussian Cox processes and shot-noise Cox processes. For spatio-temporal point pattern data, spatio-temporal log-Gaussian Cox process models have recently found different applications. Here we study and apply spatio-temporal shot-noise Cox point process models in the line suggested by [8] to model the space-time first-order intensity function







 $\log A_1(u) = c(\beta^{V,C,E}) + \sum_{j} \beta_j^{W} I[V(u) = i] + \sum_{j} \beta_j^{C} I[C(u) = j] + \beta_1^{E} E(u) + \beta_2^{E} E(u)$ $\log \lambda_2(t) = \beta_0 + \beta_1^S \cos(\eta t) + \beta_2^S \sin(\eta t) + \beta_3^S \cos(\eta t) +$ $\boldsymbol{\beta}_{i}^{S} \sin(2\boldsymbol{\eta}t) + \boldsymbol{\beta}_{i}^{T}T(t) + \boldsymbol{\beta}_{i}^{T}T(t)^{2} + \boldsymbol{\beta}_{i}^{T}T(t)^{3} + \boldsymbol{\beta}_{i}^{T}T(t)^{4} + \boldsymbol{\beta}_{i}^{T}T(t)^{5}$



Temporal Intensity (°C*10)

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